

## BRIEF COMMUNICATION

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### NMR RELAXATION OF PROTEIN AND WATER PROTONS IN METHEMOGLOBIN SOLUTIONS

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**ABSTRACT** Hemoglobin (Hb) proton spins rapidly equilibrate among themselves after an initial excitation, and relax toward thermal equilibrium as a unit. In the diamagnetic form, spin diffusion to nearby methyl relaxation sinks can account for this. For metHb, four strong heme relaxation centers dominate, and spin diffusion must occur over long distances. A sizeable difference in protein  $T_1$  is found between  $H_2O$  and  $D_2O$  solutions, much more than for diamagnetic Hb, consistent with internal  $H_2O$  acting as a spin carrier to the heme.

#### INTRODUCTION

In proton relaxation studies of diamagnetic proteins, it is striking that most spectral regions have the same longitudinal magnetization recovery rate after initial spin excitation (1). For the purposes of this study, then, we can treat all protein-proton spins as equivalent, or "well-mixed." Good mixing of solvent-water protons also occurs, because molecular diffusion is rapid, and the lifetime of a water molecule in the hydration region can be assumed to be short. Protein and water protons exchange magnetization at the protein-water interface via cross-relaxation processes (2, 3); direct transfer by proton exchange is negligible at our pH, and time scale  $\sim 0.1$  s. Thus a simple two-phase exchange formalism can be used to describe relaxation, analogous to relaxation in systems with atomic exchange (4). Magnetization of each phase relaxes as the sum of two exponentials, whose slopes and amplitudes are functions of the number of protons and the intrinsic relaxation rates in each phase, and the exchange rates between them.

Our interest here is to investigate how efficiently the protein-proton spins mix among themselves, and to probe the mechanisms involved. Individual protons have varied interactions and molecular dynamics, and some, for example methyl protons, would be expected to have faster relaxation rates than others (1). However, overall equilibration is rapid, in part due to efficient spin coupling, but mainly because differences in local relaxation rates are small, and relaxation sinks such as methyl groups are widely distributed. This equilibration can be characterized as a diffusion process, similar to thermal or atomic diffusion, and theoretical spin-diffusion constants  $D_s$  have been derived for solid-state nuclear magnetic resonance (NMR) (5). Although  $D_s$  is always many orders of magnitude slower than solvent diffusion,

any reasonable estimate (see below) would probably be adequate to smooth out local  $T_1$  variations.

The spin diffusion mechanism is more severely tested with methemoglobin, in which the heme irons are ferric, paramagnetic, and potent relaxation centers for the water spins (6). Most protein-protons are immobile and quite distant from the heme sites, and the value of  $D$ , estimated below would leave them unaffected. However, we find that for methemoglobin, protein relaxation is enhanced, and much more so in  $H_2O$  than  $D_2O$ . The latter result suggests that there is enough mobile water in the protein interior to act as a spin carrier to the ferric relaxation sinks.

## EXPERIMENTAL

Human erythrocytes were washed in isotonic saline-phosphate buffer at pH 5.7, hemolyzed by repeated freezing and thawing cycles, centrifuged (and sometimes filtered) to remove stroma or other suspended matter, and diluted to the desired protein concentration using the buffer mixture. Measurements with diamagnetic hemoglobin (Hb) were made soon after preparation, so that there was little spontaneous conversion to the met form, as indicated by the water  $T_2$ . MetHb was obtained by first incubating the red cells in 1% sodium nitrite, and then proceeding as above (7). Preparation of solutions in  $D_2O$  was similar, using reagents in 99.8%  $D_2O$ , freed of paramagnetic impurities by ion exchange. Red cells were incubated in  $D_2O$  for 24–48 h, which resulted in deuteration of most of the exchangeable protein-protons, (~20% of the total).

NMR relaxation measurements ( $T_1$  and  $T_2$ ) were made at 20 MHz, using a spectrometer described elsewhere (4). Longitudinal relaxation of a two-phase system with exchange is given in general by the sum of two exponentials (4):

$$\Delta M_p(t) = M_{p+} \exp(-\phi_{1+}t) + M_{p-} \exp(-\phi_{1-}t) \quad (1a)$$

$$\Delta M_A(t) = M_{A+} \exp(-\phi_{1+}t) + M_{A-} \exp(-\phi_{1-}t) \quad (1b)$$

$$2\phi_{1\pm} = (R_{1p} + k_s + R_{1a} + k_t) \pm [(R_{1p} + k_s - R_{1a} - k_t)^2 + 4k_s k_t]^{1/2}, \quad (2)$$

$$(\phi_{1+} - \phi_{1-})M_{p+} = (R_{1p} + k_s - \phi_{1-})\Delta M_{p0} - k_t \Delta M_{A0} \quad (3a)$$

$$(\phi_{1+} - \phi_{1-})M_{p-} = (\phi_{1+} - R_{1p} - k_s)\Delta M_{p0} + k_t \Delta M_{A0} \quad (3b)$$

$$(\phi_{1+} - \phi_{1-})M_{A+} = (R_{1a} + k_t - \phi_{1-})\Delta M_{A0} - k_s \Delta M_{p0} \quad (3c)$$

$$(\phi_{1+} - \phi_{1-})M_{A-} = (\phi_{1+} - R_{1a} - k_t)\Delta M_{A0} + k_s \Delta M_{p0} \quad (3d)$$

$$M_{p+} + M_{p-} = \Delta M_{p0} \equiv M_{p0} - M_p^0, M_{A+} + M_{A-} = \Delta M_{A0} \equiv M_{A0} - M_A^0. \quad (3e)$$

Magnetizations of the protein and water spins,  $M_p$  and  $M_A$  are expressed as deviations from equilibrium magnetizations  $M_p^0$  and  $M_A^0$ , e.g.,  $\Delta M_p = M_p - M_p^0$ . Initial values, after a preparative pulse sequence, are  $M_{p0}$  and  $M_{A0}$ . The fast and slow  $T_1$  decay rates are  $\phi_{1+}$  and  $\phi_{1-}$ , respectively, and depend on the (single) intrinsic relaxation rates of the protein and water phases,  $R_{1p}$  and  $R_{1a}$ , and average spin-transfer rates from protein to water ( $k_s$ ) and the reverse ( $k_t$ ); the latter are related through detailed balancing,  $k_s N_p = k_t N_A$ , where  $N_p$  and  $N_A$  are the proton populations of the protein and solvent phases.

The central experimental problem is to extract the two decay rates,  $\phi_{1\pm}$  from biphasic  $T_1$  decays. (In addition, it is frequently possible to obtain enough amplitude information to evaluate  $R_{1p}$ ,  $R_{1a}$ , and  $k_s$  separately.) For 2 mM protein concentrations in  $H_2O$ ,  $N_p/N_A = 0.12$ , and in a conventional  $T_1$  experiment, the fast component is barely discernible. Two techniques are used to obtain  $\phi_{1+}$  (8): (a) The spin system is initially excited with a  $90^\circ - \tau - (-180^\circ) - \tau - 90^\circ$  rf pulse triplet, where  $\tau$  is the time between pulses. Since  $T_2$  of water is ~300 ms, and the protein  $T_2$ s are ~1 ms (data not shown), a  $\tau$  of a

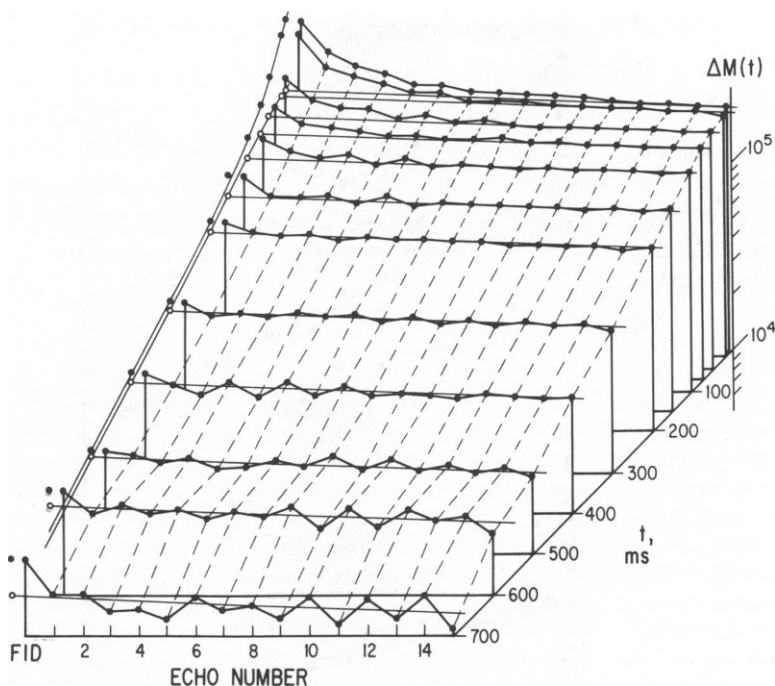


FIGURE 1 Representative magnetization recovery data for protein and water protons, monitored by a FID and spin-echo train, at various times  $t$  after an initial triplet excitation ( $\tau = 5$  ms); 2.4 mM metHb in  $\text{H}_2\text{O}$ , pH 6.0. Data points are connected as a visual aid.

few milliseconds gives  $\Delta M_{p0} \approx M_p$ ,  $\Delta M_{A0} \approx 0$ . (b) Because of the long water  $T_2$ , later echos observed in monitoring the magnetization recovery with a spin-echo sequence (9, 10) are solely due to solvent spins. Extrapolation back to the start of the echo train gives  $\Delta M_A(t)$ ;  $\Delta M_p(t)$  follows by subtraction.

Similar techniques of selective excitation and detection were used in cross-relaxation studies by Edzes and Samulski (11). Fig. 1 shows raw magnetization recovery data of 2.4 mM metHb, pH 6.0 in  $\text{H}_2\text{O}$ , with triplet excitation and an echo monitor. The first signal of each pulse train is from a 50- $\mu\text{s}$  gate beginning 50  $\mu\text{s}$  after the start of the free induction decay (FID). Subsequent gates were 200  $\mu\text{s}$ , centered on the echos, and spaced at 0.97 ms. The FID and extrapolated water signals are projected on the plane at the left, giving a graph similar to Fig. 2. In Fig. 1, the time evolution of each echo is shown by dashed lines, comprising a set of isoclines for the more distant echos. Early echos and the FID contain both protein and water signals; after subtracting  $\Delta M_A$ ,  $\Delta M_p$  alone is shown (for a different sample) in Fig. 3, for the FID and first three echos. The fast exponential dominates (Eq. 1a), yielding  $\phi_{1+}$ .

## RESULTS

Fig. 2 shows relaxation data for Hb in  $\text{H}_2\text{O}$ , and 95%  $\text{D}_2\text{O}$ . The properties of this diamagnetic case will be treated in detail elsewhere, but some are needed below. Both inversion and triplet excitation were used. Approximate formulas for  $\phi_{1+}$ ,  $\phi_{1-}$ , and  $M_{A+}$  are shown, valid for  $k_s$ ,  $k_i \ll R_{1p}$ . The difference of  $\phi_{1+}$  between  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$  solutions is only  $\sim 2 \text{ s}^{-1}$ , attributed to differences in  $k_s$ , rather than  $R_{1p}$ , and verified by the measured  $M_{A+}$ . Since  $k_s$  approaches zero for  $\text{D}_2\text{O}$  solvent,  $k_s$  in  $\text{H}_2\text{O}$  is  $\sim 2 \text{ s}^{-1}$ . For red cell suspensions, the effect of  $k_s$  can be shown directly, and is  $\sim 4 \text{ s}^{-1}$  (Fig. 4, reference 2) for such highly concentrated Hb solutions.

Fig. 3 shows  $\Delta M_p$  alone, for MetHb in  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$ , as monitored by the FID and first

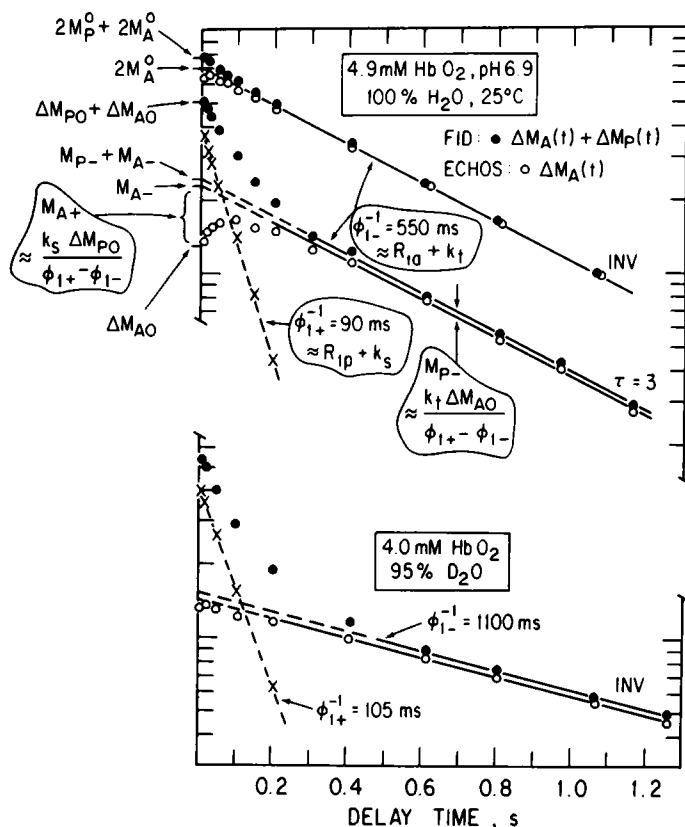


FIGURE 2  $T_1$  data for diamagnetic Hb in  $H_2O$  and  $D_2O$  after an initial inverting pulse or an  $rf$  triplet. Data are resolved into the components shown, as defined in the text.

three echo gates. Triplet excitation with  $\tau = 1, 2.5$ , and  $5$  ms was used. For a given gate, comparison of slopes was made easier by normalizing all data to the same starting value. For  $\tau = 1$ , only  $\sim 50\%$  of the protein spins are excited; nevertheless, within  $10$  ms ( $H_2O$ ) and  $30$  ms ( $D_2O$ ), all monitors of one sample show the same single exponential behavior.

A further control is obtained if azide is bound to the sixth heme ligand site, blocking water access. This greatly decreases  $R_{1r}$  and  $\phi_{1-}$ . Previous water relaxation studies (12) have shown azide-metHb to be indistinguishable from diamagnetic Hb. Although the magnetic moment of the azide complex is about half that of the aquo species, the electron relaxation time of the former is presumably much shorter. Azide binding greatly decreases  $\phi_{1+}$  also (Fig. 3), but not to its diamagnetic limit; this contrast bears further investigation.

We did not study dependences on protein concentration in any detail. Although water relaxation is very sensitive to concentration (and pH),  $\phi_{1+}$  was little affected until extreme concentrations.

## DISCUSSION

First, consider diamagnetic relaxation of hemoglobin protons in  $D_2O$  solution. Typically  $\phi_{1+}^{-1} \sim 100$  ms; this can only be due to spin interactions among the protein-protons themselves,

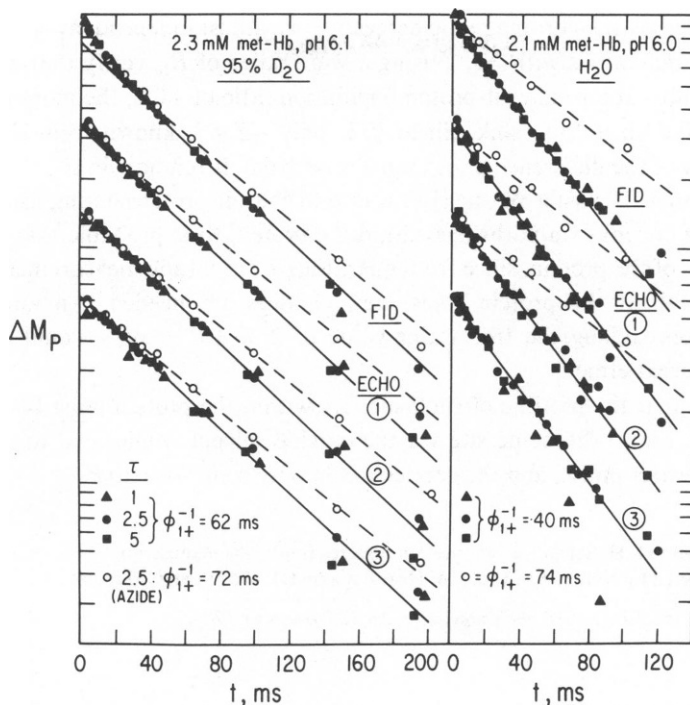


FIGURE 3 Magnetization recovery of protein-protons alone, after various triplets, for metHb in  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$ , as monitored by the FID and first three echos. For the final data, the heme sites of both samples were saturated with azide.

mediated by spin diffusion, because the solvent deuterium spins couple very weakly to the protons. For paramagnetic metHb in  $\text{D}_2\text{O}$ ,  $\phi_{1+}^{-1}$  decreases to  $\sim 60$  ms; this difference provides a quantitative measure of spin transfer between protein-protons alone, a necessary starting point before evaluating any solvent contribution.

Spin diffusion in solutions is slower than in solids, since the tumbling of the solute molecules, or their internal motions give  $T_2$  values much longer than the rigid lattice limit. We use the approximation  $D_s = a^2/30 T_2$  (5), where  $a$  is the distance between the coupled protons responsible for the process. Taking  $a = 2.5 \text{ \AA}$ , a typical distance between proton groups, and an average  $T_2 = 1.0 \text{ ms}$ ,  $D_s = 2.1 \times 10^{-14} \text{ cm}^2/\text{s}$ . The distance between ferric atoms ranges from 25 to 40  $\text{\AA}$  (13); taking 15  $\text{\AA}$  as the farthest distance of any proton from a relaxation center, and using the three dimensional diffusion formula (14)  $t = l^2/6D_s$ , the time for a spin to diffuse 15  $\text{\AA}$  is  $\sim 170 \text{ ms}$ . Considering the many approximations, this value is consistent with the measured  $R_{1p}$  in  $\text{D}_2\text{O}$ .

The contribution of spin diffusion for a solution of Hb or metHb in  $\text{H}_2\text{O}$  should be much the same as for  $\text{D}_2\text{O}$ . About 20% of the protein-protons are exchanged for deuterons in our  $\text{D}_2\text{O}$  samples, but this would make  $R_{1p}$  somewhat faster than in a 100% protonated molecule, since for well-mixed protein spins, relaxation is proportional to the ratio of protein-protons to ferric atoms.

For metHb,  $\phi_{1+}$  is  $9 \text{ s}^{-1}$  faster in  $\text{H}_2\text{O}$  than  $\text{D}_2\text{O}$ . Although solvent relaxation  $R_{1s}$  is

drastically affected by the paramagnetic hemes,  $\phi_{1+}$  is almost independent of  $R_{1a}$  at 2 mM Hb concentration. Calculations with Eq. 2 using a wide range of  $R_{1a}$  verify that  $\phi_{1+} \sim R_{1p} + k_s$ . That is, for a solute-proton/solvent-proton population ratio of  $\sim 0.1$ , the more populous water phase behaves like an infinite sink. Since  $k_s$  is only  $\sim 2 \text{ s}^{-1}$ , known from the diamagnetic experiment, most of the difference in  $\phi_{1+}$  must arise from differences in  $R_{1p}$ .

We conclude that the faster  $R_{1p}$  in  $\text{H}_2\text{O}$  is due to solvent protons acting as spin carriers to the ferric relaxation sinks via pathways within the protein. It is probable that such pathways reach all portions of the protein, since from quantitative amplitude measurements we know we measure almost all of the protein spins. Few carriers are needed. An internal diffusion constant even approaching the free water value of  $2 \times 10^{-5} \text{ cm}^2/\text{s}$  would enable a small number to have great effect.

It also follows that the lifetime of such carriers within the protein must be long compared with  $R_{1p}^{-1}$ . Any route to the heme site via the outside solvent would lead to immediate spin mixing with the water phase, and the carrier would only contribute to  $k_s$ .

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